



Bi-ideals in Ternary Seminear Rings

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ARTICLE INFO	ABSTRACT
Published Online: 14 April 2023 Corresponding Author: A. Dhivya Bharathi	In this paper, we introduce the concept of Bi-ideal in ternary seminear rings as a generalization of quasi ideals in ternary seminear rings. We also study the notion of minimal bi-ideal in ternary seminear rings and derive some of their interesting properties.
KEYWORDS: Ternary seminear ring, Regular Ternary seminear ring, Ideals in Ternary seminear ring, Quasi ideal in ternary seminear rings, Bi-ideal	
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1 INTRODUCTION

Algebraic structures take a part in very marvellous role in mathematics which classifies in many area such as control engineering, physics, computer coding, IT, control engineering, etc. In 1952, Good.R.A and Hughes.D.R [2] started the concept of bi-ideals for a semigroup. Szasz.F [14][9] generalized bi-ideals of rings in 1970. In 1983, Pilz Gunter [11] came up with an idea of near ring. Krishna.K.V. [6][7][8] brought up with near-semi rings in 2005.

Kar.S.[4] initiated on quasi-ideals and bi-ideals in ternary semi rings. Dheena.P and Elavarasan.B., [1] were studied about the prime bi-ideals in ternary semi ring. Shique Li and Young He [13] floated on semigroups whose bi-ideals are strongly prime. Iampan.A [3] studied a note on bi-ideals in T-Semigroups. Koteswaramma.N and Venkateswara Rao.J.[5] have studied on bi-ideals and Minimal bi-ideals in ternary semi ring. Many authors worked on bi-ideals [10][12].

The notion of ternary seminear rings was initiated in 2020 by us [15]. Later we worked on [16][17][18][19][20].

In this paper, we define the notion of bi-ideal in ternary seminear rings. We also introduce a minimal bi-ideal in ternary seminear rings and obtained their properties.

2 PRELIMINARIES

Definition 2.1 A ternary seminear ring is a nonempty set T together with a binary operation called addition '+' and a ternary operation called ternary multiplication denoted by juxtaposition, such that

(i) $(T, +)$ is a semigroup.

(ii) T is a ternary semigroup under ternary multiplication.

(iii) $xy(z + u) = xyz + xyu$ for all $x, y, z, u \in T$.

Definition 2.2 A ternary seminear ring T is said to have an absorbing zero if there exists an element $0 \in T$ such that
i) $x + 0 = 0 + x = x$ for all $x \in T$. ii) $xy0 = x0y = 0xy = 0$ for all $x, y \in T$.

Remark 2.3 Throughout this paper T will always stand for the ternary seminear ring will always mean that ternary seminear ring with an absorbing zero.

Definition 2.4 Let T be a ternary seminear ring. A nonempty subset R of T is said to be a ternary subseminear ring of T if R itself is a ternary seminear ring under the same operations of T .

Definition 2.5 Let T be a ternary seminear ring $(T, +, \cdot)$. A non empty subset I of T is said to be a left(lateral and right) ideal of T if it holds the following conditions i) $i + j \in I$ for all $i, j \in I$ ii) $t_1 t_2 i$ (respectively $t_1 i t_2, i t_1 t_2$) $\in I$ for all $t_1, t_2 \in T$ and $i \in I$. If I is a left, a lateral and a right ideal of T then I is said to be an ideal of T .

Definition 2.6 Let T be a ternary seminear ring. A proper ideal I of T is said to be a prime ideal if whenever $XYZ \subseteq I$ then $X \subseteq I$ or $Y \subseteq I$ or $Z \subseteq I$, for all ideals X, Y, Z of T .

Definition 2.7 Let T be a ternary seminear ring. A proper ideal I of T is said to be a semiprime ideal if whenever $X^3 \subseteq I$ then $X \subseteq I$, for any ideals X of T .

Definition 2.8 Let $(T, +, \cdot)$ be a ternary seminear ring. For all $x, y, u, v \in T$, T is called

- i) Left cancellative if $u + x = u + y \Rightarrow x = y$ and $uvx = uvy \Rightarrow x = y$
- ii) Right cancellative if $x + v = y + v \Rightarrow x = y$ and $xuv = yuv \Rightarrow x = y$
- iii) Lateral cancellative if $uxv = uyv \Rightarrow x = y$
- iv) Cancellative if T is left, right and laterally cancellative.

Definition 2.9 A congruence ρ on a ternary seminear ring T is said to be a cancellative congruence on T if T/ρ is a cancellative ternary seminear ring.

Remark 2.10 Multiplicatively cancellative (MC) means it is enough to show that the ternary cancellative operations in the cancellative ternary seminear ring (ie., we can omit the binary addition).

Definition 2.11 Let T be a ternary seminear ring. Let U be an additive subsemigroup of T . U is said to be a quasi-ideal of T if $UTT \cap (TUT + TTUTT) \cap TTU \subseteq U$.

Definition 2.12 Let $(B, +, *)$ be a semiring. A bi-ideal C is a subsemiring of B if $CBC \subseteq C$

Definition 2.13 An element x in a ternary seminear ring T is called regular if there exists an element y in T such that $xyx=x$. A ternary seminear ring T is called regular if all of its elements are regular.

Theorem 2.14 Let T be a ternary seminear ring. Then the following conditions are equivalent

- i) T is regular.
- ii) For any right ideal A , lateral ideal B , left ideal C of T , $ABC = A \cap B \cap C$.
- iii) For $x, y, z \in T$, $\langle x \rangle_r \langle y \rangle_m \langle z \rangle_l = \langle x \rangle_r \cap \langle y \rangle_m \cap \langle z \rangle_l$
- iv) For $x \in T$, $\langle x \rangle_r \langle x \rangle_m \langle x \rangle_l = \langle x \rangle_r \cap \langle x \rangle_m \cap \langle x \rangle_l$

Theorem 2.15 Let I be a ternary subsemigroup of a ternary seminear ring T . Then I is a left(lateral or right)ideal of T if and only if $TTI \subseteq I$

(respectively $TIT \subseteq I$ and $ITT \subseteq I$).

3 BI IDEALS IN TERNARY SEMINEAR RINGS

In this section we discussed about the Bi-ideals in ternary seminear rings.

Definition 3.1 Let T be a ternary seminear ring. A ternary subseminear ring V of T is said to be a bi-ideal of T if $VTVTV \subseteq V$.

Theorem 3.2 Let T be a ternary seminear ring. An intersection of an arbitrary collection of bi-ideals of T is also a bi-ideal of T .

Proof. Let $\{V_i: i \in I\}$ be an arbitrary collection of bi-ideals of a ternary seminear ring T . Let $a, b \in \bigcap_{i \in I} V_i$. Then $a, b \in V_i$

for all $i \in I$. Since every V_i is a bi-ideal of T , then we have $a + b \in V_i, \forall i \in I$ which implies that $a + b \in \bigcap_{i \in I} V_i$

Let $a, b, c \in \bigcap_{i \in I} V_i$. Then $a, b, c \in V_i$ for all $i \in I$.

Since every V_i is a bi-ideal of T , we have $a, b, c \in V_i$ for all $i \in I$ implies that $a, b, c \in \bigcap_{i \in I} V_i$. Now $V_iTV_iTV_i \subseteq V_i$ and

$\bigcap_{i \in I} V_i \subseteq V_i$ for all $i \in I$ then we have

$$\left[\bigcap_{i \in I} V_i \right] T \left[\bigcap_{i \in I} V_i \right] T \left[\bigcap_{i \in I} V_i \right] \subseteq V_iTV_iTV_i \subseteq V_i \text{ for all } i \in I.$$

Thus which implies that $\left[\bigcap_{i \in I} V_i \right] T \left[\bigcap_{i \in I} V_i \right] T \left[\bigcap_{i \in I} V_i \right] \subseteq \bigcap_{i \in I} V_i$.

Hence $\bigcap_{i \in I} V_i$ is a bi-ideal of T .

Theorem 3.3 Let T be a ternary seminear ring. Each quasi-ideal of T is a bi-ideal of T .

Proof. Let T be a ternary seminear ring. U be a quasi-ideal of T . Then

$$UTUTU \subseteq U(TTT)T \subseteq UTT,$$

$$UTUTU \subseteq T(TTT)U \subseteq TTU, \text{ and}$$

$$UTUTU \subseteq TTUTT. \text{ And } \{0\} \subseteq TUT.$$

Therefore $\{0\} + UTUTU \subseteq TUT + TTUTT$.

Hence it follows that

$$UTUTU \subseteq UTT \cap (TUT + TTUTT) \cap TTU \subseteq U.$$

and consequently U is a bi-ideal of T .

Remark 3.4 Generally V be a bi-ideal of T and W is a bi-ideal of V , then W is need not a bi-ideal of T . Yet, in specific case, we have the succeeding theorem.

Theorem 3.5 Let T be a ternary seminear ring. V be a bi-ideal of T and W be a bi-ideal of V such that $W^3 = W$. Then W is a bi-ideal of T .

Proof. As V be a bi-ideal of T , $VTVTV \subseteq V$, and W be a bi-ideal of V , then $WVWVW \subseteq W$. Consequently,

$$\begin{aligned} WTWTW &= (WWW)TWT(WWW) \\ &= WW(WTWTW)WW \\ &\subseteq WW(VTVTV)WW \\ &\subseteq WWWWW \\ &= WWVW(WWW) \\ &= W(WVWVW)W \\ &\subseteq WWW \\ &\subseteq W. \end{aligned}$$

Definition 3.6 Let T be a ternary seminear ring. $|T| \geq 2$ is said to be a ternary division seminear ring if any non zero element x in T , there exists a non zero element y of T such that $xyz = yxz = zxy = zyx = z$ for all $z \in T$.

Theorem 3.7 Let T be a ternary seminear ring. T has no non zero proper bi-ideals if T is a ternary division seminear ring.

Proof. Let T be a ternary division seminear ring and V be a non zero bi-ideal of T .

Let x be a non zero element in V .

Then there exists a non zero element t in T such that $xtz = txz = zxt = ztx = z, \forall z \in T$, which implies that $T =$

$$VTT = TTV.$$

Now

$$\begin{aligned} T &= VTT \\ &= V(TTV)(TTV) \\ &= V(VTT)(TVT)(TTV)V \\ &= V(VTVTV)V \\ &\subseteq VVV \\ &\subseteq V. \end{aligned}$$

Therefore, $T \subset V$ and $V \subset T$ which implies $V = T$ and thus T has no non zero proper bi-ideals.

Theorem 3.8 A Multiplicative Cancellative (MC) ternary seminear ring T is zero divisor.

Proof. Let T be a MC ternary seminear ring and $xyz = 0$ for $x, y, z \in T$. If $y \neq 0$ and $z \neq 0$, then by right cancellativity $xyz = 0yz = x = 0$. Similarly we can show that $y = 0$ if $x \neq 0$ and $z \neq 0$ or $z = 0$ if $x \neq 0$ and $y \neq 0$. Therefore, T is zero divisor.

Theorem 3.9 Let T be a ternary seminear ring. A, B and C be three ternary subseminear rings of T and $V = ABC$. Then, V is a bi-ideal if atleast one of A, B, C is a right, a lateral or a left ideal of T .

Proof. Let T be a ternary seminear ring and $V = ABC$. If A be a right ideal of T . Then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq A(TTT)(TTT)TTBC \\ &\subseteq A(TTT)TBC \\ &\subseteq (ATT)BC \\ &\subseteq ABC. \text{ (By Theorem 2.8)} \end{aligned}$$

Therefore $V = ABC$ is a bi-ideal of T . Again, B be a right ideal of T . Then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq AB(TTT)(TTT)TTC \\ &\subseteq AB(TTT)TC \\ &\subseteq A(BTT)C \\ &\subseteq ABC. \end{aligned}$$

Consequently $V = ABC$ is a bi-ideal of T . Now, if C be a right ideal of T , then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq (ABC)(TTT)(TTT)TT \\ &\subseteq (ABC)(TTT)T \\ &\subseteq (ABC)TT \\ &\subseteq AB(CTT) \\ &\subseteq ABC. \end{aligned}$$

Therefore $V = ABC$ is a bi-ideal of T . Similarly, if A be a left ideal of T . The

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq (TTT)(TTT)TT(ABC) \\ &\subseteq TTTTABC \\ &\subseteq (TTA)BC \\ &\subseteq ABC. \end{aligned}$$

Therefore $V = ABC$ is a bi-ideal of T . Suppose B be a left ideal of T . Then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq A(TTT)(TTT)TTBC \\ &\subseteq A(TTT)TBC \\ &\subseteq A(TTB)C \\ &\subseteq ABC \end{aligned}$$

Hence $V = ABC$ is a bi-ideal of T .

If C be a left ideal. Then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq AB(TTT)(TTT)TTC \\ &\subseteq AB(TTT)TC \\ &\subseteq AB(TTC) \\ &= ABC \end{aligned}$$

Therefore $V = ABC$ is a bi-ideal of T .

If A be a lateral ideal of T . Then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq (TTT)TA(TTT)TBC \\ &\subseteq T(TAT)TBC \\ &\subseteq (TAT)BC \\ &\subseteq ABC. \end{aligned}$$

Therefore A be a lateral ideal of T . $V = ABC$ be a bi-ideal of T .

Again B be a lateral ideal of T . Then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq A(TTT)TBT(TTT)C \\ &\subseteq AT(TBT)TC \\ &\subseteq A(TBT)C \\ &\subseteq ABC. \end{aligned}$$

Therefore $V = ABC$ be a bi-ideal of T .

Suppose C be a lateral ideal of T . Then

$$\begin{aligned} (ABC)T(ABC)T(ABC) &\subseteq AB(TTT)TCT(TTT) \\ &\subseteq ABT(TCT)T \\ &\subseteq AB(TCT) \\ &\subseteq ABC. \end{aligned}$$

Therefore $V = ABC$ be a bi-ideal of T .

Theorem 3.10 A ternary subseminear ring V of T be a bi-ideal of T if $V = ABC$, where A is a right ideal, B is a lateral ideal and C is a left ideal of T .

Proof. Let V be a ternary subseminear ring of T . Suppose $V = ABC$, where A is a right ideal, B is a lateral ideal and C is a left ideal of T , then

$$\begin{aligned} V &= (ATT)(TBT)(TTC) \forall A, B, C \in V \\ &\subseteq A(TTT)B(TTT)C \\ &\subseteq ATBTC \\ &\subseteq V \\ &= ABC. \end{aligned}$$

Therefore V is a bi-ideal of T .

Theorem 3.11 Let T be a ternary seminear ring. Let V be a ternary subseminear ring of T . If A be a right ideal, B be a lateral ideal and C be a left ideal of T such that $ABC \subseteq V \subseteq A \cap B \cap C$ then V be a bi-ideal of T .

Proof.

$$\begin{aligned} VTVTV &\subseteq (A \cap B \cap C)T(A \cap B \cap C)T(A \cap B \cap C) \\ &\subseteq A(TBT)C \\ &\subseteq ABC \\ &\subseteq V. \end{aligned}$$

Therefore V is a bi-ideal of T .

Theorem 3.12 The following criteria in a ternary seminear ring T are equivalent.

- i) T be regular.
- ii) Each bi-ideal V of T , $VTVTV = V$.
- iii) Each quasi-ideal U of T , $UTUTU = U$.

Proof. (i) \Rightarrow (ii) Suppose T is regular. Let V is a bi-ideal of T . Let $x \in V$. Then there exists an element y in T such that $xyx = x$. Thus implies that $x = xyxyx \in VTVTV$.

Therefore $V \subseteq VT V T V$. Since V is a bi-ideal of T , $V T V T V \subseteq V$. Hence $V T V T V = (ii) \Rightarrow (iii)$

Obviously it is true. $(iii) \Rightarrow (i)$

If (iii) holds. Let A be a right ideal B be a lateral ideal and C be a left ideal of T . Then $U = A \cap B \cap C$ is a quasi ideal of T (by theorem 3.3). Hence $U T U T U = U$. Suppose $A \cap B \cap C = U = U T U T U \subseteq A T B T C \subseteq A B C$. Clearly $A B C \subseteq A \cap B \cap C$. Therefore $A \cap B \cap C = A B C$ and thus from (theorem 2.7). T is a regular ternary seminear ring.

Theorem 3.13 *A ternary subseminear ring V of a regular ternary seminear ring T is a bi-ideal of $T \Leftrightarrow V = V T V$.*

Proof. If $V = V T V$, then obviously V is a bi-ideal of T . Conversely, V is a bi-ideal of a regular ternary seminear ring T . Let $x \in V$, then there exists an element y in T such that $x = x y x$. This implies that $x \in V T V$ and consequently $V \subseteq V T V$. Now, $V T V \subseteq V T V T V \subseteq V$. Therefore $V = V T V$.

Theorem 3.14 *A ternary subseminear ring V of a regular ternary seminear ring T is a bi-ideal of $T \Leftrightarrow V$ is a quasi ideal of T .*

Proof. Let T is a regular ternary seminear ring. If V is a quasi-ideal of T , then (by theorem 3.3), V is a bi-ideal of T . Conversely, let V be a bi-ideal of T (by theorem 2.7), we have T be a regular ternary seminear ring then $A \cap B \cap C = A B C$, for any right ideal A , lateral ideal B and left ideal C .

Also,

$$\begin{aligned} &V T T \cap (T V T + T T V T T) \cap T T V \\ &= V T T (T V T + T T V T T) T T V \\ &= (V T T) (T V T) (T T V) + (V T T) (T T V T T) (T T V) \\ &= V (T T T) V (T T T) V + V (T T T) T V (T T T) T V \\ &\subseteq V T V T V + V T T V T T V \\ &\subseteq V + V T V \quad (\text{by theorem 3.13}) \\ &= V + V \\ &\subseteq V. \end{aligned}$$

Therefore V is a quasi-ideal of T .

Theorem 3.15 *Let T be a ternary seminear ring. R is a ternary subseminear ring of T . If V is a bi-ideal of T then $V \cap R$ is a bi-ideal of R .*

Proof. Let T be a ternary seminear ring R be a ternary subseminear ring of T . Let $A = V \cap R \Rightarrow A \subseteq V$ and $A \subseteq R$.

Consider

$$\begin{aligned} &A R A R A \subseteq V R V R V \subseteq V T V T V \subseteq V, \\ &\text{and } A R A R A \subseteq R R R R R \subseteq R. \end{aligned}$$

Consequently, $A R A R A \subseteq V \cap R = A$.

Hence $A = V \cap R$ is a bi-ideal of R .

Theorem 3.16 *Let T be a ternary seminear ring. If V_1, V_2 and V_3 are three bi-ideals of T , then $V_1 V_2 V_3$ is a bi-ideal of T .*

Proof. Let T , be a ternary seminear ring. V_1, V_2 and V_3 are three bi-ideals of T .

$$\begin{aligned} &\Rightarrow V T V T V \subseteq V. \\ &\Rightarrow (V_1 V_2 V_3) T (V_1 V_2 V_3) T (V_1 V_2 V_3) \\ &\subseteq (V_1 T T) T (T V_2 T) T (T T V_3) \\ &\subseteq (V_1 T T) (T T V_2 T T) (T T V_3) \\ &\subseteq V_1 V_2 V_3. \end{aligned}$$

Consequently, $V_1 V_2 V_3$ be a bi-ideal of T .

Theorem 3.17 *Let T be a ternary seminear ring. If I be an ideal and U be a quasi-ideal of T then $I \cap U$ be a bi-ideal of T .*

Proof. Let T be a ternary seminear ring. I be an ideal. U be a quasi ideal of T . Clearly $I \cap U$ be a ternary subseminear ring of T .

$$\begin{aligned} &\Rightarrow (I \cap U) T (I \cap U) T (I \cap U) \\ &\subseteq (I T I T I) \cap (U T U T U) \\ &\subseteq I \cap U. \end{aligned}$$

Hence $I \cap U$ is a bi-ideal of T .

Theorem 3.18 *Let T be a ternary seminear ring. R, S be ternary subseminear ring of T , then $V = R T S$ be a bi-ideal of T .*

Proof. Let T be a ternary seminear ring. R, S be two ternary subseminear ring of T , then $V = R T S$ is a subseminear ring of T .

$$\begin{aligned} V T V T V &\subseteq (R T S) T (R T S) T (R T S) \\ &\subseteq R (T T T) (T T T) (T T T) S \\ &\subseteq R T S \\ &\subseteq V. \end{aligned}$$

Then $V = R T S$ be a bi-ideal of T .

Definition 3.19 *Let T be a ternary seminear ring. A proper bi-ideal V of T is called prime bi-ideal if $X Y Z \subseteq V$ which implies that $X \subseteq V$ or $Y \subseteq V$ or $Z \subseteq V$ for bi-ideals X, Y and Z of T .*

Definition 3.20 *Let T be a ternary seminear ring. A proper bi-ideal V of T is called semi prime bi-ideal if $X^3 \subseteq V$ which implies that $X \subseteq V$ for bi-ideal $X \in T$.*

Definition 3.21 *Let T be a ternary seminear ring. A non zero bi-ideal V of T is said to be a minimal bi-ideal of T if V does not properly contain any non zero bi-ideal.*

Theorem 3.22 *Let T be a ternary seminear ring. A is a minimal right ideal, B is a minimal lateral ideal and C is a minimal left ideal of T . Then $A B C = 0$ or $A B C$ be a minimal bi-ideal of T .*

Proof. Let T be a ternary seminear ring. A is a minimal right ideal, B is a minimal lateral ideal and C is a minimal left ideal of T . $A B C$ be an additive subseminear ring of T . Suppose $A B C \neq 0$ and let $V = A B C$. Then (by theorem 3.10), V is a bi-ideal of T .

Let X be any bi-ideal of T , such that $0 \neq X \subseteq V \subseteq A$. Then $X T T$ is a right ideal of T and $X T T \subseteq V T T = (A B C) T T \subseteq A T T \subseteq A$. As A be a minimal right ideal of T . Consequently $X T T = 0$ or $X T T = A$.

If $X T T = 0$ then $X = A$ and $A B C = 0$ this makes

a contradiction. Consequently $XTT = A$.

Similarly, we can show $TXT = B$ and $TTX = C$.
Consequently $V = ABC = XTXTXTX \subseteq XTXTX \subseteq X$.
Therefore $V = X$. Thus ABC be a minimal bi-ideal of T .

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