

Star Related V_4 Cordial graphs

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Abstract:

Let $\langle A, * \rangle$ be any abelian group. A graph $G = (V(G), E(G))$ is said to be A -cordial[6] if there is a mapping $f: V(G) \rightarrow A$ which satisfies the following two conditions with each edge $e = uv$ is labeled as $f(u)*f(v)$.

$$(i) |v_f(a) - v_f(b)| \leq 1, \forall a, b \in A$$

$$(ii) |e_f(a) - e_f(b)| \leq 1, \forall a, b \in A$$

where $v_f(a)$ = the number of vertices with label a

$v_f(b)$ = the number of vertices with label b

$e_f(a)$ = the number of edges with label a

$e_f(b)$ = the number of edges with label b

We note that if $A = \langle V_4, * \rangle$ is a multiplicative group. Then the labeling is known as **V_4 Cordial Labeling**. A graph is called a **V_4 Cordial graph** if it admits a V_4 Cordial Labeling.

In this paper, It is proved that $Z-(P_n)$, Book and $K_{1,1,n}$ are **V_4 Cordial graphs**.

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Keywords and Phrases: Cordial labeling, V_4 Cordial Labeling and V_4 Cordial Graph.

1.Introduction:

By a graph, it means a finite undirected graph without loops or multiple edges. For graph theoretic terminology, we referred Harary [4]. For labeling of graphs, we referred Gallian[1].

A vertex labeling of a graph G is an assignment of labels to the vertices of G that induces for each edge uv a label depending on the vertex labels of u and v .

A graph G is said to be labeled if the n vertices are distinguished from one another by symbols such as v_1, v_2, \dots, v_n . In a labeling of a particular type, the vertices are assigned distinct values from a given set, which induces distinguish edge values satisfying certain conditions. The concept of graceful labeling was introduced by Rosa[3] in 1967 and subsequently by Golomb[2]. In this paper, It is proved that $Z-(P_n)$, Book and $K_{1,1,n}$ are **V_4 Cordial graphs**.

2.Preliminaries

Definition 2.1:

Let $G = (V, E)$ be a simple graph. Let $f: V(G) \rightarrow \{0, 1\}$ and for each edge uv , assign the label $|f(u) - f(v)|$. f is called a **cordial labeling** if the number of vertices labeled 0 and the the number of vertices labeled 1 differ by atmost

1 and also the number of edges labeled 0 and the the number of edges labeled 1 differ by atmost 1. A graph is called **Cordial** if it has a cordial labeling.

Definition 2.2:

Let $\langle A, * \rangle$ be any abelian group. A graph $G = (V(G), E(G))$ is said to be A -cordial if there is a mapping $f: V(G) \rightarrow A$ which satisfies the following two conditions with each edge $e = uv$ is labeled as $f(u)*f(v)$.

- (i) $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in A$
- (ii) $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in A$

where $v_f(a)$ = the number of vertices with label a .

$v_f(b)$ = the number of vertices with label b .

$e_f(a)$ = the number of edges with label a .

$e_f(b)$ = the number of edges with label b .

It is note that if $A = \langle V_4, * \rangle$ is a multiplicative group. Then the labeling is known as **V₄ Cordial Labeling**. A graph is called a **V₄ Cordial graph** if it admits a V₄ Cordial Labeling.

Definition 2.3:

Z-(P_n) is a graph obtained by, in a pair of path P_n , in which i^{th} vertex of a path P_1 is joined with $i+1^{th}$ vertex of a path P_2 .

Definition 2.4[1]:

Define the product $G_1 \times G_2$ by, consider any two vertices $u = (u_1, u_2)$, and $v = (v_1, v_2)$ in $V_1 \times V_2$. Then u and v are adjacent in $G_1 \times G_2$ whenever $(u_1 = v_1 \text{ and } u_2 \text{ adj to } v_2)$ or $(u_2 = v_2 \text{ and } u_1 \text{ adj to } v_1)$.

The product $P_m \times P_n$ is called polar grids and $K_2 \times P_n$ is called Ladder.

The product $C_m \times P_n$ is called Grids on cylinder of order mn . In particular, $D_n = C_n \times K_2$ is called a prism and $B_m = K_{1,m} \times K_2$ is called a **book**.

Definition 2.5:

K_{1,1,n} is a graph obtained by attaching root of a star $K_{1,n}$ at one end of P_2 and other end is joined with each pendant vertex of $K_{1,n}$.

3.Main Results:

Theorem 3.1.

$Z-(P_n)$ is a V_4 Cordial graph.

Proof:

Let $V(Z-(P_n)) = \{u_i, v_i : 1 \leq i \leq n\}$.

Let $E(Z-(P_n)) = \{(u_i u_{i+1}) : 1 \leq i \leq n-1\} \cup \{(v_i u_{i+1}) : 1 \leq i \leq n\} \cup \{(v_i v_{i+1}) : 1 \leq i \leq n-1\}$.

Define $f : V(Z-(P_n)) \rightarrow V_4$ by

$$f(u_i) = \begin{cases} -1 & \text{if } i \equiv 0,3 \pmod{8} \\ -i & \text{if } i \equiv 1,6 \pmod{8} \\ i & \text{if } i \equiv 2,5 \pmod{8} \\ 1 & \text{if } i \equiv 4,7 \pmod{8} \end{cases}, \quad 1 \leq i \leq n$$

$$f(v_i) = \begin{cases} -i & \text{if } i \equiv 0,3(\text{mod } 8) \\ 1 & \text{if } i \equiv 1,6(\text{mod } 8) \\ -1 & \text{if } i \equiv 2,5(\text{mod } 8) \\ i & \text{if } i \equiv 4,7(\text{mod } 8) \end{cases}, 1 \leq i \leq n$$

The induced edge labelings are

$$f(u_i)*f(u_{i+1}) = \begin{cases} i & \text{if } i \equiv 0(\text{mod } 4) \\ 1 & \text{if } i \equiv 1(\text{mod } 4) \\ -i & \text{if } i \equiv 2(\text{mod } 4) \\ -1 & \text{if } i \equiv 3(\text{mod } 4) \end{cases}, 1 \leq i \leq n-1$$

$$f(v_i)*f(u_{i+1}) = \begin{cases} -1 & \text{if } i \equiv 0(\text{mod } 4) \\ i & \text{if } i \equiv 1(\text{mod } 4) \\ 1 & \text{if } i \equiv 2(\text{mod } 4) \\ -i & \text{if } i \equiv 3(\text{mod } 4) \end{cases}, 1 \leq i \leq n-1$$

$$f(v_i)*f(v_{i+1}) = \begin{cases} -i & \text{if } i \equiv 0(\text{mod } 4) \\ -1 & \text{if } i \equiv 1(\text{mod } 4) \\ i & \text{if } i \equiv 2(\text{mod } 4) \\ 1 & \text{if } i \equiv 3(\text{mod } 4) \end{cases}, 1 \leq i \leq n-1$$

Vertex Conditions:

- (i) $v_f(1) = v_f(i) = v_f(-i) = v_f(-1) = \frac{n}{2}$, when $n \equiv 0(\text{mod } 2)$
- (ii) $v_f(1) = v_f(-i) = \frac{n+1}{2}$ and $v_f(i) = v_f(-1) = \frac{n-1}{2}$, when $n \equiv 1(\text{mod } 8)$
- (iii) $v_f(1) = v_f(i) = \frac{n-1}{2}$ and $v_f(-i) = v_f(-1) = \frac{n+1}{2}$, when $n \equiv 3(\text{mod } 8)$
- (iv) $v_f(1) = v_f(-i) = \frac{n-1}{2}$ and $v_f(i) = v_f(-1) = \frac{n+1}{2}$, when $n \equiv 5(\text{mod } 8)$
- (v) $v_f(1) = v_f(i) = \frac{n+1}{2}$ and $v_f(-i) = v_f(-1) = \frac{n-1}{2}$, when $n \equiv 7(\text{mod } 8)$

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

- (i) $e_f(i) = e_f(-1) = e_f(-i) = 3\left(\frac{n}{4} - 1\right) + 2$ and $e_f(1) = 3\left(\frac{n}{4} - 1\right) + 3$, when $n \equiv 0(\text{mod } 4)$
- (ii) $e_f(1) = e_f(i) = e_f(-1) = e_f(-i) = 3\left(\frac{n-1}{4}\right)$, when $n \equiv 1(\text{mod } 4)$
- (iii) $e_f(1) = e_f(i) = e_f(-1) = 3\left(\frac{n-2}{4}\right) + 1$ and $e_f(-i) = 3\left(\frac{n-2}{4}\right)$, when $n \equiv 2(\text{mod } 4)$
- (iv) $e_f(1) = e_f(i) = 3\left(\frac{n-3}{4}\right) + 2$ and $e_f(-1) = e_f(-i) = 3\left(\frac{n-3}{4}\right) + 1$, when $n \equiv 3(\text{mod } 4)$

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, $Z-(P_n)$ is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of $Z-(P_3)$, $Z-(P_4)$, $Z-(P_5)$, $Z-(P_6)$, $Z-(P_7)$, $Z-(P_9)$ are shown in Figures 3.1.1-3.1.6.

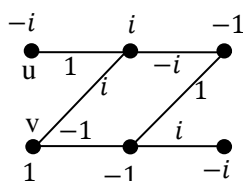


Figure 3.1.1

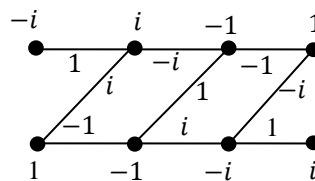


Figure 3.1.2

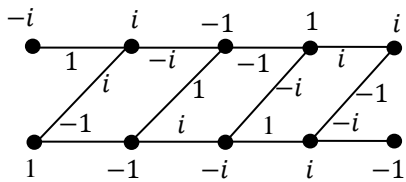


Figure 3.1.3

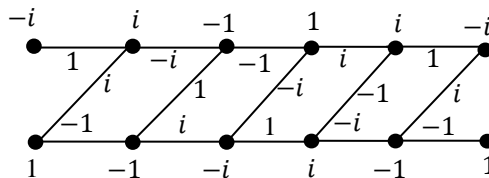


Figure 3.1.4

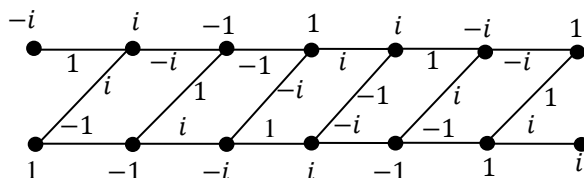


Figure 3.1.5

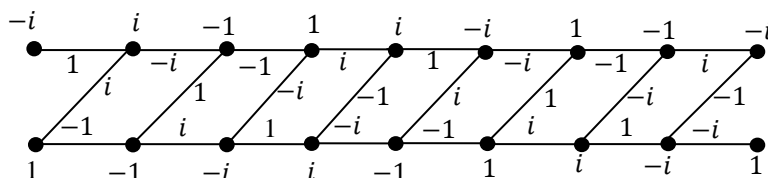


Figure 3.1.6

Theorem 3.2.

Book is a V_4 Cordial graph.

Proof:

Let $(V(G)) = \{u, w, v_i : 1 \leq i \leq n\}$.

Let $(E(G)) = \{(uv_i) : 1 \leq i \leq n\} \cup \{(wv_i) : 1 \leq i \leq n\}$.

Define $f : V(G) \rightarrow V_4$ by

Case(i): when $n \equiv 0 \pmod{4}$

Let $f(u) = -1, f(w) = 1$

$$f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -i & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

The induced edge labelings are

Let $f(u) * f(w) = -1$

$$f(u) * f(v_i) = \begin{cases} -1 & \text{if } i \equiv 0 \pmod{4} \\ i & \text{if } i \equiv 1 \pmod{4} \\ -i & \text{if } i \equiv 2 \pmod{4} \\ 1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

$$f(w) * f(v_i) = 1 = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -i & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

Vertex Conditions:

Here, $v_f(1) = v_f(-1) = \frac{n}{4} + 1$ and $v_f(i) = v_f(-i) = \frac{n}{4}$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

Here, $e_f(1) = e_f(i) = e_f(-i) = \frac{n}{2}$ and $e_f(-1) = \frac{n}{2} + 1$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, Book is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of Book is shown in the Figure 3.2.1.

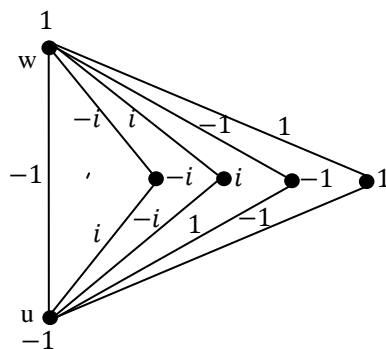


Figure 3.2.1

Case(ii): when $n \equiv 1 \pmod{4}$

Let $f(u) = i, f(w) = -1$

$$f(v_i) = \begin{cases} -1 & \text{if } i \equiv 0 \pmod{4} \\ 1 & \text{if } i \equiv 1 \pmod{4} \\ -i & \text{if } i \equiv 2 \pmod{4} \\ i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

The induced edge labelings are

Let $f(u) * f(w) = -i$

$$f(u) * f(v_i) = \begin{cases} -i & \text{if } i \equiv 0 \pmod{4} \\ i & \text{if } i \equiv 1 \pmod{4} \\ 1 & \text{if } i \equiv 2 \pmod{4} \\ -1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

$$f(w) * f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

Vertex Conditions:

Here, $v_f(1) = v_f(-1) = v_f(i) = \frac{n-1}{4} + 1$ and $v_f(-i) = \frac{n-1}{4}$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

Here, $e_f(1) = \frac{n-1}{2}$ and $e_f(i) = e_f(-1) = e_f(-i) = \frac{n-1}{2} + 1$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, Book is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of Book is shown in the Figure 3.2.2.

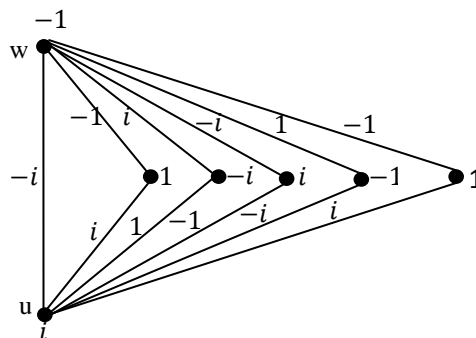


Figure 3.2.2.

Case(iii): when $n \equiv 2 \pmod{4}$

Let $f(u) = i$, $f(w) = 1$, $f(v_n) = -1$

$$f(v_i) = \begin{cases} i & \text{if } i \equiv 0 \pmod{4} \\ -i & \text{if } i \equiv 1 \pmod{4} \\ 1 & \text{if } i \equiv 2 \pmod{4} \\ -1 & \text{if } i \equiv 3 \pmod{4} \end{cases} , 1 \leq i \leq n - 1$$

The induced edge labelings are

Let $f(u) * f(w) = i$, $f(u) * f(v_n) = -i$ and $f(w) * f(v_n) = -1$

$$f(u) * f(v_i) = \begin{cases} -1 & \text{if } i \equiv 0 \pmod{4} \\ 1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases} , 1 \leq i \leq n - 1$$

$$f(w) * f(v_i) = \begin{cases} i & \text{if } i \equiv 0 \pmod{4} \\ -i & \text{if } i \equiv 1 \pmod{4} \\ 1 & \text{if } i \equiv 2 \pmod{4} \\ -1 & \text{if } i \equiv 3 \pmod{4} \end{cases} , 1 \leq i \leq n - 1$$

Vertex Conditions:

Here, $v_f(1) = v_f(-1) = v_f(i) = v_f(-i) = \frac{n-2}{4} + 1$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

$e_f(1) = e_f(i) = e_f(-1) = \frac{n-2}{2} + 1$ and $e_f(-i) = \frac{n-2}{2} + 2$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, Book is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of Book is shown in the Figure3.2.3.

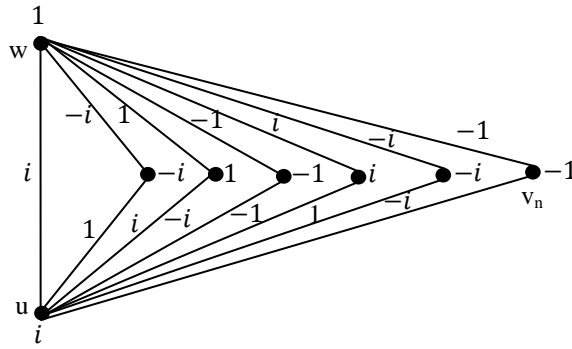


Figure 3.2.3

Case(iv): when $n \equiv 3 \pmod{4}$

Let $f(u) = 1, f(w) = -i$

$$f(v_i) = \begin{cases} -i & \text{if } i \equiv 0 \pmod{4} \\ i & \text{if } i \equiv 1 \pmod{4} \\ -1 & \text{if } i \equiv 2 \pmod{4} \\ 1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

The induced edge labelings are

Let $f(u) * f(w) = -i$

$$f(u) * f(v_i) = \begin{cases} -i & \text{if } i \equiv 0 \pmod{4} \\ i & \text{if } i \equiv 1 \pmod{4} \\ -1 & \text{if } i \equiv 2 \pmod{4} \\ 1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

$$f(w) * f(v_i) = \begin{cases} -1 & \text{if } i \equiv 0 \pmod{4} \\ 1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

Vertex Conditions:

Here, $v_f(1) = \frac{n+1}{4} + 1$ and $v_f(-1) = v_f(i) = v_f(-i) = \frac{n+1}{4}$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

Here, $e_f(1) = e_f(i) = e_f(-i) = \frac{n+1}{2}$ and $e_f(-1) = \frac{n+1}{2} - 1$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, Book is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of Book is shown in the Figure3.2.4.

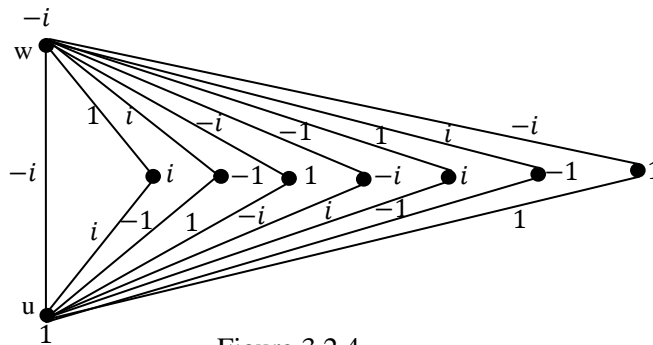


Figure 3.2.4

Theorem 3.3.

$K_{1,1,n}$ is a V_4 Cordial graph .

Proof:

Let $V(K_{1,1,n}) = \{u, v, v_i : 1 \leq i \leq n\}$.

Let $E(K_{1,1,n}) = \{(uv) : 1 \leq i \leq n\} \cup \{(uv_i) : 1 \leq i \leq n\} \cup \{(vv_i) : 1 \leq i \leq n\}$.

Define $f : V(K_{1,1,n}) \rightarrow V_4$ by

Case(i): when $n \equiv 0 \pmod{4}$

Let $f(u) = -1, f(v) = 1$

$$f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

The induced edge labelings are

Let $f(u) * f(v) = -1$

$$f(u) * f(v_i) = \begin{cases} -1 & \text{if } i \equiv 0 \pmod{4} \\ 1 & \text{if } i \equiv 1 \pmod{4} \\ -i & \text{if } i \equiv 2 \pmod{4} \\ i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

$$f(v) * f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

Vertex Conditions:

Here, $v_f(1) = v_f(-1) = \frac{n}{4} + 1$ and $v_f(i) = v_f(-i) = \frac{n}{4}$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

Here, $e_f(1) = e_f(i) = e_f(-i) = \frac{n}{2}$ and $e_f(-1) = \frac{n}{2} + 1$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, $K_{1,1,n}$ is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of $K_{1,1,4}$ is shown in the Figure 3.3.1.

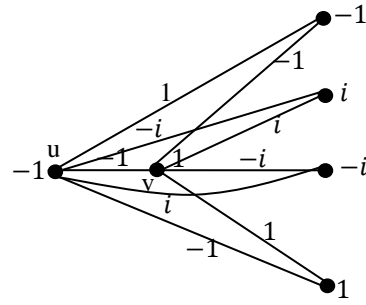


Figure 3.3.1

Case(ii): when $n \equiv 1 \pmod{4}$

Let $f(u) = i, f(v) = 1$

$$f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

The induced edge labelings are

Let $f(u) * f(v) = i$

$$f(u) * f(v_i) = \begin{cases} i & \text{if } i \equiv 0 \pmod{4} \\ -i & \text{if } i \equiv 1 \pmod{4} \\ -1 & \text{if } i \equiv 2 \pmod{4} \\ 1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

$$f(v) * f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

Vertex Conditions:

Here, $v_f(1) = v_f(-1) = v_f(i) = \frac{n-1}{4} + 1$ and $v_f(-i) = \frac{n-1}{4}$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

Here, $e_f(1) = \frac{n-1}{2}$ and $e_f(i) = e_f(-1) = e_f(-i) = \frac{n+1}{2}$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, $K_{1,1,n}$ is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of $K_{1,1,5}$ is shown in the Figure3.3.2.

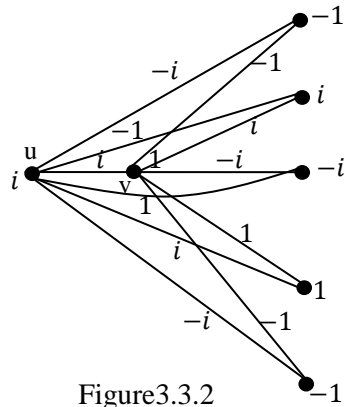


Figure3.3.2

Case(iii): when $n \equiv 2 \pmod{4}$

Let $f(u) = -i, f(v) = 1$

$$f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

The induced edge labeling are

Let $f(u) * f(v) = -i$

$$f(u) * f(v_i) = \begin{cases} -i & \text{if } i \equiv 0 \pmod{4} \\ i & \text{if } i \equiv 1 \pmod{4} \\ 1 & \text{if } i \equiv 2 \pmod{4} \\ -1 & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

$$f(v) * f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

Vertex Conditions:

Here, $v_f(1) = v_f(-1) = v_f(i) = v_f(-i) = \frac{n-2}{4} + 1$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

(i) $e_f(1) = e_f(-i) = e_f(-1) = \frac{n}{2}$ and $e_f(i) = \frac{n+2}{2}$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, $K_{1,1,n}$ is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of $K_{1,1,6}$ is shown in the

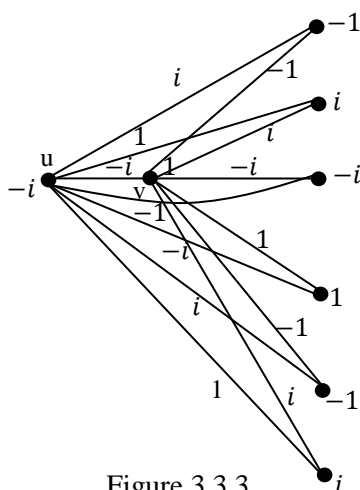


Figure 3.3.3

Figure3.3.3.

Case(iv): when $n \equiv 3 \pmod{4}$

Let $f(u) = 1, f(v) = 1$

$$f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

The induced edge labelings are

Let $f(u) * f(v) = 1$

$$f(u) * f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

$$f(u) * f(v_i) = \begin{cases} 1 & \text{if } i \equiv 0 \pmod{4} \\ -1 & \text{if } i \equiv 1 \pmod{4} \\ i & \text{if } i \equiv 2 \pmod{4} \\ -i & \text{if } i \equiv 3 \pmod{4} \end{cases}, 1 \leq i \leq n$$

Vertex Conditions:

Here, $v_f(1) = \frac{n+1}{4} + 1$ and $v_f(-1) = v_f(i) = v_f(-i) = \frac{n+1}{4}$.

Hence, $|v_f(a) - v_f(b)| \leq 1, \forall a, b \in V_4$.

Edge Conditions:

Here, $e_f(i) = e_f(-1) = e_f(-i) = \frac{n+1}{2}$ and $e_f(1) = \frac{n-1}{2}$.

Hence, $|e_f(a) - e_f(b)| \leq 1, \forall a, b \in V_4$.

Hence, $K_{1,1,n}$ is a V_4 Cordial Graph .

For example, the V_4 Cordial Labeling of $K_{1,1,7}$ is shown in the Figure3.3.4.

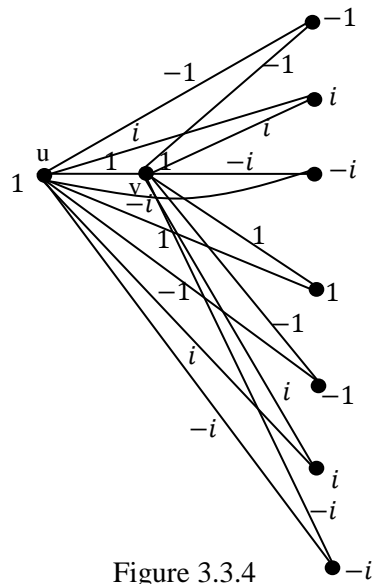


Figure 3.3.4

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